

Continuous random variables A1 MS

Q1.

1 (i) 1/12	B1 [1]	Accept 0.0833
(ii) trains arrive every 12 minutes	B1 [1]	must have 'every 12 minutes'

Q2.

7	(i)	$\int_{-1}^1 k(1-x)dx = 1$ $(k[x - \frac{x^2}{2}]_{-1}^1 = 1)$ $2k = 1$ $(k = \frac{1}{2} \quad \mathbf{AG})$	M1 A1 [2]	Attempt integ $f(x) = 1$ with correct limits
	(ii)	$(\int_{0.5}^1 \frac{1}{2}(1-x)dx = \frac{1}{2}[x - \frac{x^2}{2}]_{0.5}^1)$ $= \frac{1}{16} \text{ or } 0.0625$	B1 [1]	
	(iii)	$\int_{-1}^1 \frac{1}{2}(x-x^2)dx$ $= \frac{1}{2}[\frac{x^2}{2} - \frac{x^3}{3}]_{-1}^1$ $= -\frac{1}{3} \text{ or } -0.333$	M1 A1 A1 [3]	$\int xf(x)dx$ ignore limits Correct integrand and limits
	(iv)	$\int_{-1}^a \frac{1}{2}(1-x)dx = 0.25$ $(\frac{1}{2}[x - \frac{x^2}{2}]_{-1}^a = 0.25)$ $(\frac{1}{2}(a - \frac{a^2}{2} - (-1 - \frac{1}{2})) = 0.25)$ $a^2 - 2a - 2 = 0$ $a = 1 - \sqrt{3} \text{ or } -0.732$	M1 A1 A1 [3]	Correct limits (or integral from a to 1 = 0.75) any correct QE with “= 0”(or in completed square form $(a-1)^2 = 3$) Not $a = 1 \pm \sqrt{3}$; Not -0.732 or 2.732
[Total: 9]				

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Q3.

<p>5 (i) $\int_1^{\infty} \frac{k}{x^4} dx = 1$ $\left[-\frac{k}{3x^3} \right]_1^{\infty} = 1$ oe $(0 + \frac{k}{3} = 1 \Rightarrow k = 3 \quad \mathbf{AG})$</p>	<p>M1 A1 [2]</p>	<p>Attempt integ $f(x)$ & “= 1”; ignore limits Correct integrand & limits leading to AG, no errors seen</p>
<p>(ii) $\int_1^{\infty} x \times \frac{3}{x^4} dx$ $\left[-\frac{3}{2x^2} \right]_1^{\infty}$ $= \frac{3}{2}$ $\int_1^{\infty} x^2 \times \frac{3}{x^4} dx$ $\left[-\frac{3}{x} \right]_1^{\infty} (= 3)$ “3” – $\left(\frac{3}{2} \right)^2$ $= \frac{3}{4}$</p>	<p>M1 A1 M1* A1 M1*dep A1 [6]</p>	<p>Attempt integ $xf(x)$; ignore limits. CWO Attempt integ $x^2f(x)$; ignore limits. Correct integrand; correct limits dep 2nd M1 attempt $E(X^2) - [E(X)]^2$ cwo</p>

Q4.

<p>4</p>	<p>(i) $0.5(0.5 + 0.75) \times 0.5$ or $\int_1^{1.5} \frac{x}{2} dx$ $= \frac{5}{16}$ or 0.3125 or 0.313</p>	<p>M1 A1 [2]</p>	<p>Attempt find correct area eg 1 squ + $\frac{1}{4}$ squ or integral with correct limits any $f(x)$</p>
	<p>(ii) $\frac{1}{2}m \times \frac{m}{2}$ or $\int_0^m \frac{x}{2} dx$ $= \frac{1}{2}$ $m = \sqrt{2}$ or 1.41</p>	<p>M1 M1 A1 [3]</p>	<p>Attempt area from 0 to m (or m to 2) their $f(x)$ Expression for area = $\frac{1}{2}$. Ignore limits</p>
	<p>(iii) $\int_0^2 \frac{x^2}{2} dx$ $= \frac{4}{3}$ oe</p>	<p>M1 A1 [2]</p>	<p>Attempt $\int xf(x) dx$. Ignore limits</p>

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Q5.

6	(i)	$-k \int_2^3 (x^2 - 5x + 6) dx = 1$ $(-k(\frac{3^3}{3} - 5 \times \frac{3^2}{2} + 6 \times 3 - [\frac{2^3}{3} - 5 \times \frac{2^2}{2} + 6 \times 2]) = 1)$ $-k \times (-\frac{1}{6}) = 1 \text{ or } k \times \frac{1}{6} = 1$ $(k = 6 \text{ AG})$	M1 A1 [2]	Integ = 1; ignore limits Correctly obtain $-\frac{1}{6}$ or $\frac{1}{6}$ CWO No rounded decimals	$-6 \int_2^3 (x^2 - 5x + 6) dx$ ignore limits Correctly obtain 1
	(ii)	$E(X) = 2.5$ $-6 \int_2^3 (x^4 - 5x^3 + 6x^2) dx \quad (= -6 \times (-1.05))$ $- "2.5" ^2$ $= 0.05$	B1 M1* Dep M1* A1 [4]	Condone 25000 Integ $x^2 f(x)$; ignore limits Subtr μ^2 , ISW	
	(iii)	$-6 \int_2^{2.2} (x^2 - 5x + 6) dx \quad (= 0.104)$ $1 - (1 - "0.104")^4$ $= 0.355/0.356$	M1 M1 A1 [3]	Integ with limits 2, 2.2 or 2.2, 3 Or equivalent	
[Total: 9]					

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Q6.

7 (i) (a) X or 5	B1 [1]	
(b) V or 3 Higher and lower values more likely or there are more higher and lower values or more prob at both extremes	B1 B1 dep [2]	Should mention values or prob Not just graph or spread eg not "More spread"
(ii) $\frac{2+1}{2} \times 0.5$ or $\int_0^{0.5} (2-2x) dx$ $= 0.75$	M1 A1 [2]	('or' method requires linear function and correct limits) CWO
(iii) (a) $\int_0^1 ax^n dx = 1$ $\left[\frac{ax^{n+1}}{n+1} \right]_0^1 = 1$ $\frac{a}{n+1} = 1$ ($a = n + 1$ AG)	M1 A1 A1 [3]	Attempt integ of correct form = 1 (ignore limits) Correct integrand & limits No errors seen
(b) $\int_0^1 ax^{n+1} dx = \frac{5}{6}$ oe $\left[\frac{ax^{n+2}}{n+2} \right]_0^1 = \frac{5}{6}$ oe $\frac{a}{n+2} = \frac{5}{6}$ ($6a = 5n + 10$) $a = 5, n = 4$	M1* A1 M1dep A1 [4]	Integral of form $\int xf(x) dx = \frac{5}{6}$, ignore limits Correct integrand & limits Attempt to use $a = n + 1$ within 2 nd equ to get an equ in n (or a)