

Discrete Random Variables 2 MS

Q1.

<p>6 (i) $(0.75)^n < 0.06$</p> <p>$n > 9.78$</p> <p>$n = 10$</p>	<p>M1*</p> <p>M1dep*</p> <p>A1 [3]</p>	<p>Equation or inequality with 0.75^n and 0.06 or 0.94 seen</p> <p>Attempt at solving by trial and error (can be implied) or using logarithms correctly</p> <p>Correct answer</p>
<p>(ii) $E(X) = 14 \times 0.75$ or 10.5</p> <p>Try $P(10) = {}^{14}C_{10}(0.75)^{10}(0.25)^4 = 0.220$</p> <p>$P(11) = {}^{14}C_{11}(0.75)^{11}(0.25)^3 = 0.240$</p> <p>(mode is) 11</p> <p>OR</p>	<p>M1</p> <p>M1</p> <p>A1 [3]</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>Evaluating binomial probability for an integer value directly above or below their mean</p> <p>Evaluating the other binomial probability</p> <p>Correct answer</p> <p>Evaluating binomial $P(n)$ and $P(n+1)$</p> <p>Evaluating binomial $P(10)$, $P(11)$ and $P(12)$</p> <p>Correct answer</p>
<p>(iii) $P(> 11)$</p> <p>$= {}^{14}C_{12}(0.75)^{12}(0.25)^2 + {}^{14}C_{13}(0.75)^{13}(0.25)^1 + (0.75)^{14}$</p> <p>$= 0.281$</p> <p>$P(3) = {}^5C_3 (0.281)^3(0.7189)^2$</p> <p>$= 0.115$</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 [5]</p>	<p>A binomial term of the form ${}^{14}C_n p^n (1-p)^{14-n}$ seen, $n \neq 0$ or 14</p> <p>Summing binomial $P(12, 13, 14)$ or $P(11, 12, 13, 14)$</p> <p>Correct answer 0.280 – 0.282</p> <p>A binomial term of the form ${}^5C_3 p^3 (1-p)^2$ seen, any p</p> <p>Correct answer</p>

Q2.

<p>3 (i) $P(X=1) = P(\text{GBBB}) 4 \times C_1$</p> <p>$= 5/8 \times 3/7 \times 2/6 \times 1/5 \times 4 = 1/14$</p> <p>$P(X=2) = P(\text{GGBB}) \times {}_4C_2 = 3/7$</p> <p>$P(X=3) = P(\text{GGGB}) \times {}_4C_3 = 3/7$</p> <p>$P(X=4) = P(\text{GGGG}) \times {}_4C_4 = 1/14$</p> <p>OR</p> <p>$P(1) = {}_5C_1 / {}_8C_4 = 1/14$</p> <p>$P(2) = {}_3C_2 \times {}_5C_2 / {}_8C_4 = 3/7$</p> <p>$P(3) = {}_3C_1 \times {}_5C_3 / {}_8C_4 = 3/7$</p> <p>$P(4) = {}_5C_4 / {}_8C_4 = 1/14$</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1 [4]</p>	<p>Considering values of X of 1, 2, 3, 4</p> <p>Attempting to find the probability of at least 2 values of X</p> <p>One correct probability</p> <p>All correct</p> <p>Considering values of X of 1, 2, 3, 4</p> <p>Dividing by ${}_8C_4$</p> <p>One correct probability</p> <p>All correct</p>
<p>(ii) $\text{Var}(X) = 1/14 + 12/7 + 27/7 + 16/14 - (5/2)^2$</p> <p>$= 15/28 (0.536)$</p>	<p>M1</p> <p>A1 [2]</p>	<p>Using a variance formula correctly with mean^2 subtracted numerically, no extra division</p> <p>Correct final answer</p>

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Q3.

5 (i) $4p + p + 3p = 1$ so $P(\text{blue}) = 1/8$ AG (ii) $P(R) = 1/2, P(B) = 1/8, P(G) = 3/8$ $P(\text{all different}) = 1/2 \times 1/8 \times 3/8 \times 3!$ $= 9/64$ (0.141)	B1	[1]	Must show something
	M1 M1 A1	[3]	Multiplying $P(R, B, G)$ together Mult by 3! Correct answer
(iii) mean = $136 \times 1/8 = 17$, var = 14.875 $P(<20) = P\left(z < \frac{19.5 - 17}{\sqrt{14.875}}\right)$ $= \Phi(0.648)$ $= 0.742$	B1 M1 M1 M1 A1	[5]	Unsimplified mean and variance correct Standardising, need sq rt Cont correction 19.5 or 20.5 Correct area, > 0.5 legit Correct answer

Q4.

3 (i) $P(3m) = 4/5$ (0.8) $P(5m) = 1/5$ (0.2) $E(X) = 17/5$ (3.4) $\text{Var}(X) = 16/25$ (0.64)	B1		$P(3m) = 4/5$ or $P(5m) = 1/5$ seen or implied
	B1 M1		Correct $E(X)$ Subtract their mean ² numerically from $\sum x^2 p$, no extra dividing
	A1	[4]	Correct answer
(ii) $P(3, 5) + P(5, 3) = 0.8 \times 0.2 + 0.2 \times 0.8$ $= 8/25$ (0.32)	M1 A1√	[2]	Summing two 2-factor terms Correct answer, ft on $2 \times p \times (1 - p)$, their p
(iii) $P(11) = P(3, 3, 5) + P(3, 5, 3) + P(5, 3, 3)$ $= (4/5 \times 4/5 \times 1/5) \times 3$ $= 48/125$ (0.384)	M1 M1 A1	[3]	Mult 2 probs for 3 with 1 prob for 5 Multiplying probs for 11 by 3 or summing 3 options Correct final answer

Q5.

3 (i) $p = 0.1$ (ii) (a) $P(X=1, Y=3) = 0.3 \times 0.2 = 0.06$ $P(X=2, Y=2) = 0.15 \times 0.5 = 0.075$ $P(X=3, Y=1) = 0.3 \times 0.3 = 0.09$ $P(\text{sum is 4}) = 0.225$ (b) $P(X=1, Y=\text{anything}) = 0.3$ $P(X=2, Y=\text{anything}) = 0.15$ $P(X=3, Y=1, 2) = 0.3 \times 0.8 = 0.24$ $P(X=4, Y=1) = 0.2 \times 0.3 = 0.06$ $P(X=5, Y=1) = 0.05 \times 0.3 = 0.015$ $P(\text{product} < 8) = 0.765$ OR $P(Y=1, X=\text{anything}) = 0.3$ $P(Y=2, X=1, 2, 3) = 0.5 \times 0.75 = 0.375$ $P(Y=3, X=1, 2) = 0.2 \times 0.45 = 0.09$ $P(\text{product} < 8) = 0.765$	B1	[1]	
	M1 B1		Summing 2 or 3 options One option correct unsimplified
	A1	[3]	correct final answer
	M1 B1		Σ 3 or more two-factor options Two correct options
	A1	[3]	Correct answer
	M1 B1 A1		

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Q6.

<p>4 (i) $P(X < 5) = 1 - P(5, 6, 7)$ $= 1 - (0.21)^5(0.79)^2 {}_7C_5 - (0.21)^6(0.79)^1 {}_7C_6$ $- (0.21)^7$ $= 0.994$</p> <p>(ii) $P(\text{at least } 1) = 1 - P(0) = 1 - (0.79)^7$ $= 0.808$ $P(\text{exactly } 3 \text{ weeks}) = (0.808)^3(0.192) {}_4C_3$ $= 0.405$</p>	<p>M1 A1 A1 [3] M1 A1 M1 A1 [4]</p>	<p>Binomial expression with powers $\Sigma 7$ and probs $\Sigma = 1$, and ${}_7C_r$ Correct unsimplified expression Correct answer</p> <p>Attempt to find $P(\text{at least } 1)$ or $1 - P(0 \text{ and } 1)$ Rounding to correct answer Bin expression with powers $\Sigma 4$ and their 0.808 etc. and ${}_4C_3$ Correct answer</p>
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Q7.

<p>2 (i)</p> <table border="1" style="margin-left: 20px; border-collapse: collapse; text-align: center;"> <tr> <td style="padding: 2px 10px;">y</td> <td style="padding: 2px 10px;">0</td> <td style="padding: 2px 10px;">2</td> <td style="padding: 2px 10px;">4</td> </tr> <tr> <td style="padding: 2px 10px;">$P(Y = y)$</td> <td style="padding: 2px 10px;">0.42</td> <td style="padding: 2px 10px;">0.48</td> <td style="padding: 2px 10px;">0.1</td> </tr> </table> <p>(ii) $0.96 + 0.4 = 1.36$</p>	y	0	2	4	$P(Y = y)$	0.42	0.48	0.1	<p>B1 M1 A1 A1 [4] B1ft [1]</p>	<p>0, 2, 4 only seen for Y no probs needed. Accept other vals if $P(\text{value}) = 0$ seen in table, allow 0002244 with probs Summing two or more 2-factor probs (can be implied) One correct prob Correct table or list Ft their table for Y or $X \Sigma p = 1$</p>
y	0	2	4							
$P(Y = y)$	0.42	0.48	0.1							

Q8.

<p>4 (i) mean = $11/6$ ($1 \frac{5}{6}$, 1.83) $sd = \sqrt{(1+1+1+4+9+9)/6 - (11/6)^2}$ $= \sqrt{29}/6$ (0.898)</p> <p>(ii)</p> <table border="1" style="margin-left: 20px; border-collapse: collapse; text-align: center;"> <tr> <td style="padding: 2px 10px;">x</td> <td style="padding: 2px 10px;">2</td> <td style="padding: 2px 10px;">3</td> <td style="padding: 2px 10px;">4</td> <td style="padding: 2px 10px;">5</td> <td style="padding: 2px 10px;">6</td> </tr> <tr> <td style="padding: 2px 10px;">Pr</td> <td style="padding: 2px 10px;">9/36</td> <td style="padding: 2px 10px;">6/36</td> <td style="padding: 2px 10px;">13/36</td> <td style="padding: 2px 10px;">4/36</td> <td style="padding: 2px 10px;">4/36</td> </tr> </table> <p>(iii) $p = 1/3$ $np = 8 \quad n = 24$ $\text{Var} = 24 \times 1/3 \times 2/3 = 16/3$ (5.33)</p>	x	2	3	4	5	6	Pr	9/36	6/36	13/36	4/36	4/36	<p>B1 M1 A1 [3] B1 B1 M1 A1 [4] B1 M1 A1ft [3]</p>	<p>correct answer numerical use of a correct sd/variance formula correct answer all correct x values $P(2)$ and $P(6)$ correct considering more than 1 case for a sum of 3 or 4 or 5 $P(3)$, $P(4)$ and $P(5)$ correct correct p using $np = 8$ to find n or $8(1 - p)$ to find var, $0 < p < 1$ correct answer, ft their p</p>
x	2	3	4	5	6									
Pr	9/36	6/36	13/36	4/36	4/36									

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Q9.

<p>3 (i) $z = -1.036 = \frac{73 - 75}{\sigma}$ $\sigma = 1.93$</p>	<p>B1 M1 A1 [3]</p>	<p>\pm correct z value accept ± 1.037 Equation with 73, 75, σ and a z value Rounding to correct answer</p>
<p>(ii) $P(> 77) = 0.15$ $P(< 3) = P(0, 1, 2)$ $= (0.85)^8 + {}_8C_1(0.15)(0.85)^7 + {}_8C_2(0.15)^2(0.85)^6$ $= 0.895$</p>	<p>M1 M1 A1 [3]</p>	<p>Prob rounding to 0.15 and 0.85 ${}_8C_x p^x (1-p)^{8-x}$ seen any $p, 0 < p < 1$ Correct answer</p>