

# Circular Measure 2 MS

Q1.

<b>2</b>	<b>(i)</b> $\frac{1}{2} \cdot 3^2 \pi = \frac{1}{2} 9^2 \theta - \frac{1}{2} 3^2 \theta$ $\rightarrow \theta = \frac{1}{4} \pi$	M1 A1 A1	[3]	M1 needs $\frac{1}{2} r^2 \theta$ once. A1 all correct. Answer given
	<b>(ii)</b> $P = 6 + 6 + 3 \times \frac{1}{4} \pi + 9 \times \frac{1}{4} \pi = 21.4 \text{ cm.}$ or $12 + 3\pi$	M1 A1	[2]	M1 is for use of $s = r\theta$ once.

Q2.

<b>6</b>	<b>(i)</b> $r(2\pi - \alpha) + 2r\alpha + 2r$ $2\pi r + r\alpha + 2r$	B1B1 B1 <sup>✓</sup>	[3]	fit for $r\alpha$ instead of $2r\alpha$ or omission $2r$ SC1 for $2r\alpha + 4r$ . (Plate = shaded part)
	<b>(ii)</b> $\frac{1}{2}(2r)^2 \alpha + \pi r^2 - \frac{1}{2} r^2 \alpha$ $\frac{3r^2 \alpha}{2} + \pi r^2$	B1B1 B1	[3]	Either B1 can be scored in (iii)
	<b>(iii)</b> $\pi r^2 - \frac{1}{2} r^2 \alpha = 2r^2 \alpha$ $\alpha = \frac{2}{5} \pi$	M1 A1	[2]	For equating <i>their</i> 2 parts from (ii)

Q3.

<b>2</b>	<b>(i)</b> slant length = 10 cm. circumference of base = $12\pi$ arc length = $10\theta$ (= $12\pi$ ) $\rightarrow \theta = 1.2\pi$ or 3.77 radians.	B1 B1 B1 <sup>✓</sup> B1	[4]	Use of $r\theta$ , $\theta$ calculated, not 6 or 8.
	<b>(ii)</b> $\frac{1}{2} r^2 \theta = 188.5 \text{ cm}^2$ or $60\pi$ .	M1 A1 <sup>✓</sup>	[2]	Use of $\frac{1}{2} r^2 \theta$ with radians and $r =$ calculated '10', not 6 or 8.

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Q4.

<p><b>6 (i)</b> <math>\text{area } \Delta = \frac{1}{2} \times 4 \times 4 \tan \alpha</math> oe soi</p> <p>Area sector <math>= \frac{1}{2} \times 2^2 \alpha</math> oe soi</p> <p>Shaded area <math>= 8 \tan \alpha - 2\alpha</math> cao</p> <p><b>(ii)</b> <math>DC = \frac{4}{\cos \alpha} - 2</math> oe soi</p> <p>Arc <math>DE = 2\alpha</math> soi anywhere provided clear</p> <p>Perimeter <math>= \frac{4}{\cos \alpha} + 4 \tan \alpha + 2\alpha</math> cao</p>	<p><b>B1</b></p> <p><b>B1</b></p> <p><b>B1</b></p> <p style="text-align: center;"><b>[3]</b></p> <p><b>B1</b></p> <p><b>B1</b></p> <p><b>B1</b></p> <p style="text-align: center;"><b>[3]</b></p>	<p><math>4 \tan \alpha = \sqrt{16 / \cos^2 \alpha - 16}</math> . (Can also score in answer) Accept <math>\theta</math> throughout</p> <p>Little/no working – accept terms in answer</p> <p><math>\frac{4}{\cos \alpha} = \sqrt{16 + 16 \tan^2 \alpha}</math> . Can score in answer</p> <p>Little/no working – accept terms in answer</p>
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Q5.

<p><b>2</b></p>	<p>Radius of semicircle <math>= \frac{1}{2} AB = r \sin \theta</math></p> <p>Area of semicircle <math>= \frac{1}{2} \pi r^2 \sin^2 \theta = A_1</math></p> <p>Shaded area = semicircle – segment</p> <p><math>= A_1 - \frac{1}{2} r^2 2\theta + \frac{1}{2} r^2 \sin 2\theta</math></p>	<p><b>B1</b></p> <p><b>B1</b>✓</p> <p><b>B1B1</b></p> <p style="text-align: center;"><b>[4]</b></p>	<p>aef</p> <p>Uses <math>\frac{1}{2} \pi r^2</math> with <math>r = f(\theta)</math></p> <p><b>B1</b> (–sector), <b>B1</b> for + (triangle)</p>
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Q6.

<p><b>7</b></p>	<p><b>(i)</b> <math>BC^2 = r^2 + r^2 = 2r^2 \rightarrow BC = r\sqrt{2}</math></p> <p><b>(ii)</b> Area sector <math>BCFD = \frac{1}{4} \pi (r\sqrt{2})^2</math> soi</p> <p>Area <math>\Delta BCAD = \frac{1}{2} (2r)r</math></p> <p>Area segment <math>CFDA = \frac{1}{2} \pi r^2 - r^2</math> .oe</p> <p>Area semi-circle <math>CADE = \frac{1}{2} \pi r^2</math></p> <p>Shaded area <math>\frac{1}{2} \pi r^2 - \left( \frac{1}{2} \pi r^2 - r^2 \right)</math></p> <p>or <math>\pi r^2 - \left( \frac{1}{2} \pi r^2 + \left( \frac{1}{2} \pi r^2 - r^2 \right) \right)</math></p> <p><math>= r^2</math></p>	<p><b>B1</b></p> <p style="text-align: center;"><b>[1]</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>B1</b></p> <p><b>DM1</b></p> <p><b>A1</b></p> <p style="text-align: center;"><b>[6]</b></p>	<p><b>AG</b></p> <p>Expect <math>\frac{1}{2} \pi r^2</math></p> <p>Expect <math>r^2</math> (could be embedded)</p> <p>Depends on the area <math>\Delta BCD</math></p>
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Q7.

<b>4 (i)</b>	Sector $OCD = \frac{1}{2}(2r)^2\theta (=2r^2\theta)$	<b>B1</b>	$2r^2\theta$ seen somewhere
	Sector(s) $OAB/OEF = (2)\frac{1}{2}r^2(\pi - \theta)$	<b>B1</b>	Accept with/without factor (2)
	Total $= r^2(\pi + \theta)$	<b>B1</b>	<b>AG www</b>
<b>(ii)</b>	Arc $CD = 2r\theta$	<b>B1</b>	[3]
	Arc(s) $AB/EF = (2)r(\pi - \theta)$	<b>B1</b>	Accept with/without factor (2)
	Straight edges $= 4r$	<b>B1</b>	Must be simplified
	Total $2\pi r + 4r$ (which is independent of $\theta$ )	<b>B1</b>	[4]

Q8.

<b>6 (i)</b>	$PT = r \tan \alpha$	<b>B1</b>	
	$QT = OT - OQ = \frac{r}{\cos \alpha} - r$	<b>B1</b>	
	or $\sqrt{r^2 + r^2 \tan^2 \alpha} - r$	<b>B1</b>	
	Perimeter = sum of the 3 parts including $r\alpha$	<b>B1</b>	[3]
<b>(ii)</b>	Area of triangle $= \frac{1}{2} \times 10 \times 10 \tan \frac{\pi}{3}$	<b>M1</b>	Correct formula used, $50\sqrt{3}, 86.6$
	Area of sector $= \frac{1}{2} \times 10^2 \times \frac{1}{3}\pi$	<b>M1</b>	Correct formula used, $\frac{50\pi}{3}, 52.36$
	Shaded region has area 34 (2sf)	<b>A1</b>	[3]

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Q9.

<b>6</b>	$BAC = \sin^{-1}(3/5)$ or $\cos^{-1}(4/5)$ or $\tan^{-1}(3/4)$ $ABC = \sin^{-1}(4/5)$ or $\cos^{-1}(3/5)$ or $\tan^{-1}(4/3)$  $ACB = \pi/2$ (Allow $90^\circ$ ) Shaded area = $\Delta ABC$ – sectors ( $AEF + BEG + CFG$ ) $\Delta ABC = \frac{1}{2} \times 4 \times 3$ oe Sum sectors = $\frac{1}{2} [3^2 \cdot 0.6435] +$ $2^2 \cdot 0.9273 + 1^2 \cdot 1.5708]$  <b>OR</b> $\frac{\pi}{360} [3^2 \cdot 36.8(7) + 2^2 \cdot 53.1(3) + 1^2 \cdot 90]$ $6 - 5.536 = 0.464$	<b>B1</b> <b>B1</b>  <b>B1</b> <b>M1</b> <b>B1</b>  <b>M1</b>  <b>A1</b> [7]	Accept $36.8(7)^\circ$ Accept $53.1(3)^\circ$
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